

# Stability Analysis of Hydrodynamic Journal Bearing Under Micropolar Lubrication

Dharmender<sup>1</sup>, Jaideep Gupta<sup>1</sup>

<sup>1</sup>Department of Mechanical Engineering, NIT Kurukshetra, Haryana, 136119, India

## ABSTRACT

*The lubricant available commercially, behave like non-Newtonian fluids due to the presence of different kind of additives. The characteristics of finite width hydrodynamic journal bearings lubricated with micropolar fluids are confronted. The modified Reynolds equation is incurred by applying micropolar lubrication theory. The modified Reynold equation is solved for the half Sommerfeld boundary condition. The stability in term of critical mass and eccentricity is obtained. The results show the comparison of the stability of the Newtonian fluids and the micropolar fluids. Results show that the stability is more if micropolar fluids are used. The microrotation near the surfaces of the bearing enhances the bearing pressure capacity and the stability.*

**Keywords:** *Micropolar Lubricant, Stability, Short Bearing.*

## I INTRODUCTION

In the age of technical development, the market flooded with the engineered lubricant. These lubricants contain suspended additives. Thus the classical continuum theory is unable of calculating proper flow behavior of such fluids. This leads to the generalization of Reynold equation according to the flow properties of these fluids. A new Reynold equation that takes into account all possible variation in boundary viscosity and microrotation near the surface is driven [1]. Micropolar fluids obtained from the general microfluidic by imposing the assumption of gyration tensor and microisotropic property that still exhibit microstructure. These fluids only exhibit microrotational effects and support surface and body couples [2]. Das S. et al. [3] used first-order perturbation of the film thickness and steady state film pressure, the dynamic characteristics in term of stiffness and damping coefficients; critical mass is obtained concerning micropolar property for varying eccentricity ratios and slenderness ratios. Wan Cai et al. [4] applied micropolar lubrication theory on short bearing approximation. The spatial displacement of the rotor in horizontal and vertical directions are considered for various nondimensional speed ratios. The stability of the system varies with the nondimensional speed ratios. The rotor center trajectory had undesired vibrations. The center stability is calculated.

Mathematically, for an unstable system, the level of vibration goes to infinity. There is a possible system failure, or system behavior enters nonlinear regime at higher amplitude level, vibration does not reach infinite levels. The

Dynamic instability the amplitude grows instability becomes unbounded with time if linear stability theory holds. The damping and stiffness properties of the lubricant effect the stability of the journal in bearing. In this work the critical mass parameter depends upon the damping and stiffness is calculated for the dynamic stability of the journal. The parameter calculated for both Newtonian and micropolar fluids.

## II MATHEMATICAL MODELING OF SHORT HYDRODYNAMIC JOURNAL BEARING

In hydrodynamic journal bearing consist of the journal surrounded by a enveloped called bearing. In Fig. 1 shows the schematic diagram of the journal bearing.

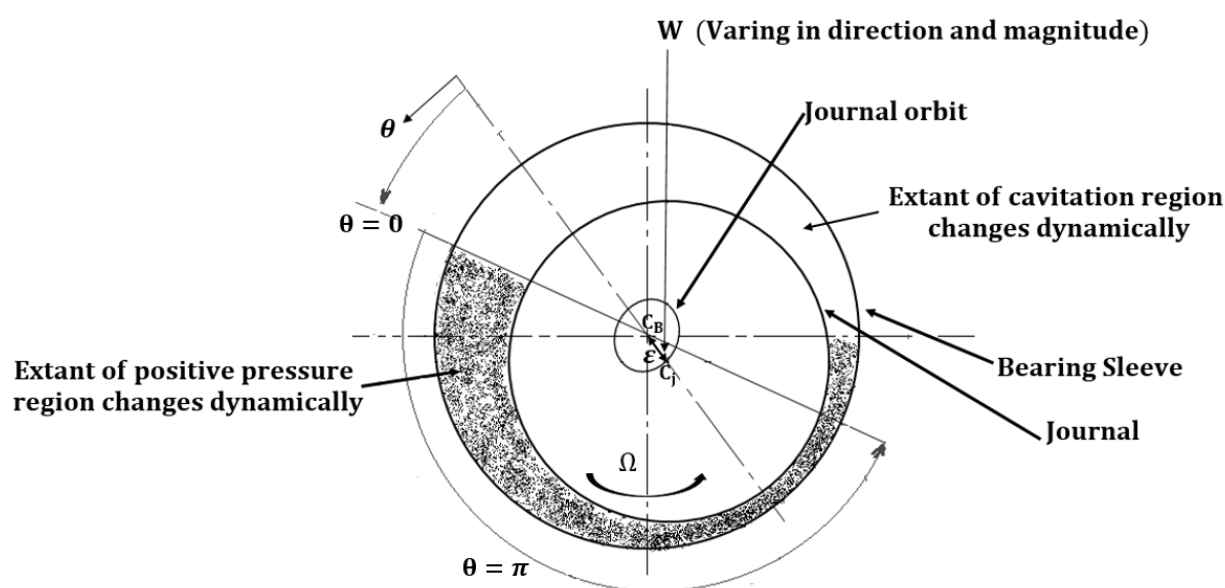


Fig 1 Schematic diagram of hydrodynamic journal bearing

The equation for the critical mass developed by considering the continuum theory of micropolar fluids.

Critical mass is defined by

$$M_I = \frac{(D_{xx}D_{yy} - D_{xy}D_{yx})}{\left[ \frac{(D_{xx}+D_{yy})(K_{xx}K_{yy} - K_{xy}K_{yx})}{K_{xx}D_{yy} + K_{yy}D_{xx} - K_{yx}D_{xy} - K_{xy}D_{yx}} - \frac{K_{yx}D_{xy} + K_{yy}D_{yy} + K_{xx}D_{xx} + K_{xy}D_{yx}}{D_{xx} + D_{yy}} \right]} \quad (1)$$

$$M_{II} = \frac{(D_{xx}D_{yy} - D_{xy}D_{yx})}{K_{xx} + K_{yy}} \quad (2)$$

Where,  $D_{xx}$ ,  $D_{yy}$ ,  $D_{yx}$ , and  $D_{xy}$  are the damping coefficient of the micropolar fluid in the horizontal and vertical axis direction and there coupled damping in both the direction. The  $K_{xx}$ ,  $K_{yy}$ ,  $K_{yx}$ , and  $K_{xy}$  are the stiffness coefficient in the horizontal and vertical axis direction.

$$M_{\text{critical}} = \min (M_I \text{ or } M_{II}) \quad \text{When } K_{xx} + K_{yy} < 0$$
$$= \min (M_I) \quad \text{When } K_{xx} + K_{yy} > 0$$

The values of the stiffness and damping coefficient are depended upon the eccentricity  $\varepsilon$ .

The eccentricity defined as

$$\varepsilon = C_B - C_j \quad (3)$$

Where  $C_B$  and  $C_j$  are bearing center and journal centers respectively.

### III RESULT AND DISCUSSION

For solving the above equation, the advanced numerical methods are employed, and the MatLab is used for the getting the results. Two cases are discussed here for different short bearing dimension. The above equation is nondimensionalized to make the computation easier. The equation is solved by forwarding difference method. The step size of 0.1. Used and the length of iteration is the length of the matrix of meshes.

#### CASE I

The bearing geometrical parameters for input are considered the  $l=3.5$  nondimensional characteristic length of the bearing. Viscosity is taken for Newtonian, and the micropolar fluid for the microstructural properties nearly nondimensional viscosity for the micropolar fluid is 0.3. The width to diameter ratio of the bearing is taken as 1 for the finite and short bearing.  $N^2=0.577$  called coupling number. Coupled the viscosity property of Newtonian and micropolar fluids. The logarithmic critical mass is calculated for the different eccentricity ratios. Fig. 2 is showing the variation of the logarithm critical mass with eccentricity for the half Sommerfeld boundary condition. In Fig. 2. The yellow line shows the threshold limit of the stable condition to the unstable condition from the results are showing that the at lower eccentricity values the value of critical mass for the Newtonian and micropolar fluids are much lower than the instability threshold. After the value of eccentricity increases from more than 0.6 the value of critical mass parameter increases rapidly and maximum between 0.7 to 0.8 eccentricity value. From the results under micropolar lubrication, the bearing provides more stability in comparison of the Newtonian lubrication.

#### CASE II

The bearing geometrical parameters for input are considered the  $l=3.5$  nondimensional characteristic length of the bearing. Viscosity is taken for Newtonian, and the micropolar fluid for the microstructural properties nearly nondimensional viscosity for the micropolar fluid is 0.3. The width to diameter ratio of the bearing taken as  $\pi/10$  for the finite and short bearing.  $N^2=0.577$  called coupling number. Coupled the viscosity property of Newtonian and micropolar fluids.

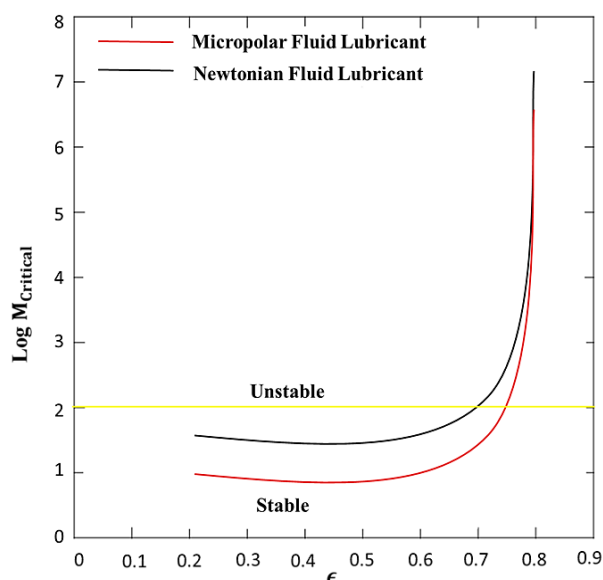


Fig. 2

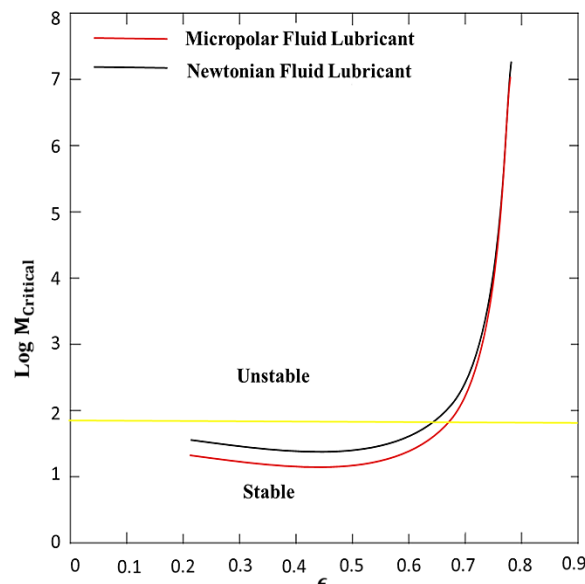


Fig. 3

Fig. 2 Critical mass V/S eccentricity for the finite length short bearing of slenderness ratio of 1

Fig. 3. Critical mass V/S eccentricity for the finite length short bearing of slenderness ratio of  $\pi/10$

The logarithmic critical mass is calculated for the different eccentricity ratios. Fig. 3. is showing the variation of the logarithm critical mass with eccentricity for the half Sommerfeld boundary condition. In Fig. 3. The yellow line shows the threshold limit of the stable condition to the unstable condition from the results are showing that at lower eccentricity values the value of critical mass for the Newtonian and micropolar fluids are much lower than the instability threshold. After the value of eccentricity increases from more than 0.6 the value of critical mass parameter increases rapidly and maximum between 0.7 to 0.8 eccentricity value. From the results under micropolar lubrication, the bearing provides more stability in comparison of the Newtonian lubrication.

#### IV CONCLUSION

The stability is the main issue related to the journal in the bearing. The instability in the rotor causes the failure of the structure and the system. The analysis of the bearing done for the micropolar and Newtonian fluid lubrication and following conclusion is drawn:

The stability is dependent upon the eccentricity of the journal under load.

The stability is also dependent upon the damping and the stiffness properties of the lubricant in horizontal and the vertical direction of the bearing.

The change in the dimension of the bearing is also crucial for the stability of the bearing.

The micropolar fluid lubricant is more stable than the Newtonian fluid lubricant in the hydrodynamic journal bearing.

The future work can be conducted for load-bearing capacity of the bearing.

## **REFERENCES**

- [1] Bassonov, N.M., A new generalization of the Reynold equation for a micropolar fluid and its application to bearing theory, *Tribology International*, 27, 1994,105-108.
- [2] Huang, T. W., Weng, C. I., Chen, C. K., Analysis of finite width journal bearing with micropolar fluids, *Wear*, 123,1988, 1-12.
- [3] Das, S., Guha, S.K., Chattopadhyay, A.K., Linear stability analysis of hydrodynamic journal bearing under micropolar lubrication, *Tribology International*,38, 2005,500-507.
- [4] Chang-Jian, C.W., Chen, C.K., Nonlinear dynamic analysis of a flexible rotor supported by micropolar fluid film journal bearing, *International Journal of Engineering Science*, 44, 2006,1050-1070.