

A REVIEW ON A NOVEL DELAY & QUANTUM COST EFFICIENT REVERSIBLE REALIZATION OF RAM

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ABSTRACT

As the conventional irreversible logic dissipates power for losing bits of information, computing engines has to be designed that do not require energy dissipation but only if computation is done logically reversible. Hence, research on reversible logic has been extensively increased now-a-days for its application in Quantum Computing, nanotechnology; QCA and Low power VLSI etc. In this paper we are using three basic 2x2 reversible logic gates. The Controlled-Not gate - commonly called the Feynman gate - is designed to produce the following output states: $P = A$ and $Q = A \oplus B$. While approaching for RRAM we have also proposed a reversible D Flip-flop with minimum quantum cost (Qc). Since fanout is expressively forbidden in reversible logic, since a fanout has one input and two outputs, the Feynman gate may be used to duplicate a signal when B is equal to 0.

Keywords: Arithmetic operations, Reversible logics, Quantum Cost Efficient, Reversible logic gates.

I. INTRODUCTION

The need and importance of quantum circuits in the area of quantum computing was first realized by Feynman in 1982 where he had shown that quantum mechanical systems cannot be efficiently simulated in a classical computer. Later in 1985 David Deutch had proposed a design of universal quantum Turing machine and provided an algorithm which proved that quantum computer can solve certain problems faster than their classical counterpart. The legacy continued for the last 25 years and in the domain of quantum computing several new possibilities appeared which are impossible in classical domain. The present work aims to add some new ideas to the existing knowledge of synthesis, optimization, testing and applications of reversible circuits and quantum circuits. It is an interesting and motivating topic since in recent past reversible computation has emerged as a promising technology having applications in low power CMOS, nanotechnology, optical computing, optical information processing, DNA computing bioinformatics, digital signal processing etc. To establish the relevance of reversible and quantum computing it would be justified to note that the VLSI industry is moving at high speed towards miniaturization. With miniaturization it faces two issues i) A considerable amount of energy gets dissipated in VLSI circuits and ii) the size of the transistors are approaching quantum limits where tunneling and other quantum phenomena are likely to appear. Thus we need a superior technology that can overcome these problems. The basic principle of reversible computing is that a injective device with an identical number of input and output lines will produce a computing environment where the electrostatics of

the system allow for prediction of all future states based on known past states, and the system reaches every possible state, resulting in no heat dissipation.

Since ancient times, humanity has been seeking tools to help us perform tasks which involve calculations. Such are computing the area of a land, computing the stresses on rods in bridges, or finding the shortest route from one place to another. A common feature of all these tasks is their structure:

Input ---> *Computation* ---> *Output*

The computation part of the process is inevitably performed by a dynamical physical system, evolving in time. In this sense, the question of what can be computed is intermingled with the physical question of which systems can be physically realized. If one wants to perform a certain computation task, one should seek the appropriate physical system, such that the evolution in time of the system corresponds to the desired computation process. If such a system is initialized according to the input, its final state will correspond to the desired output. These facts have motivated to do the present work in which studied different perspectives of synthesis, optimization and testing of reversible and quantum circuits.

II. REVERSIBLE CIRCUIT MODEL

Reversible circuit is composed of reversible logic gates. The logic gates used in conventional circuit or digital designing is irreversible (except IDENTITY and NOT gate) that means that the input cannot be traced from output. For example, the AND gate, OR gate, NAND gate etc. are irreversible gates.

A reversible circuit is represented by network of wires that carry bit values to gates that perform elementary operations on the bits. The wires are referred to as bit lines. The input bits are written on the left side of the circuit and the output bits are written on the right side of the circuit. The circuit is acyclic i.e. it is linear and time in circuit propagates from left to right. At every time step each wire can enter at most one gate, The target appear as \oplus and control appear as \bullet on the bit line also called wire which are horizontal lines that carry the bit. The state of the bit can be 0 or 1. Figure 2.1 illustrated a reversible circuit. The first bit line and second bit line are the input bits while the third bit line is a constant input (extra bit added to achieve reversibility) with input value 0. At the output the first and second bit line are garbage outputs which are no longer required for computation and the third bit line gives the desired output. A considerable amount of interesting work has already been reported in the field of synthesis, optimization, evaluation and testing of reversible circuits.

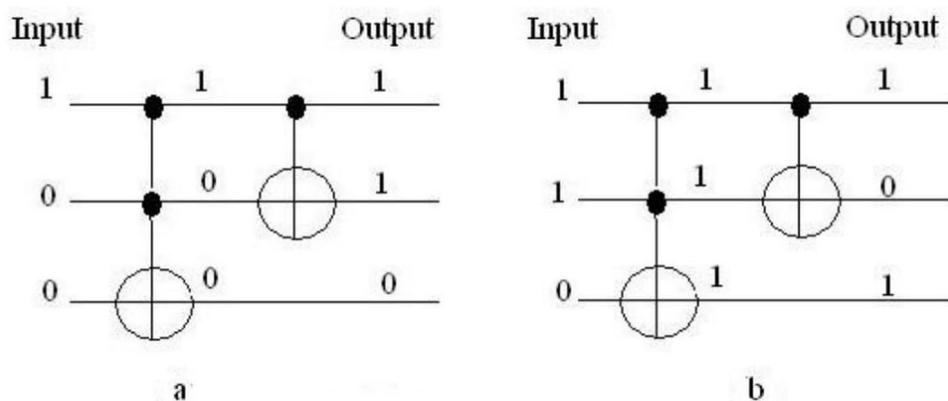


Figure 2.1 Typical Reversible circuit of a Half Adder.

A. Basic Idea of Quantum

To understand quantum circuits first need to understand the meaning of a qubit and how it differs from a bit. The Physics of quantum computing is quantum mechanics and take the liberty to choose the linear algebra model or the Dirac notation. Dirac's notation is known as *bra – ket* notation. In this notation a state vector is written as $|\psi\rangle$ which is pronounced as ket ψ . The dual of this state is the conjugate of the state vector ψ and is denoted as $\langle\psi|$ which is pronounced as bra ψ . In this notation the quantum states are represented by vectors in a complex finite dimensional vector space called inner product space) Hilbert space. The beauty of quantum circuit lies in the fact that it can perform certain tasks which are impossible in the classical world. For example, we can consider teleportation and super dense coding.

B. Gate Count (circuit cost)

Gate count is the total number of gates in a circuit. It is a quantitative measure of quality of a circuit and often referred as circuit cost. It is not unique. If one is allowed to introduce a new gate or if a complex gate library is used then the gate count can be considerably reduced. For example, let us consider the Half Adder circuit shown in Figure 2.1. It is implemented using 2 gates therefore its gate count is 2. Now we can put the two gates in a box and consider the box as a new gate. The gate count in that situation is 1. It is important to understand that each reversible gate is represented by a unitary matrix, the new gate will have a new unitary matrix formed from matrix multiplication of CCnot and Cnot therefore this new gate will solely perform as a reversible Half Adder under special condition that it's third bit value remains 0. Thus if one is allowed to introduce a new gate or a complex gate library then the gate count can be considerably reduced. This may be clearly understood for quantum gate perspective since reversible gate is only a special case of quantum gate.

C. Garbage Bits

Garbage bits are the additional output that makes a function reversible and is not used for further computations. Since the garbage bits are not used for further computation hence large number of garbage bits is not desirable in a reversible circuit. In a reversible function, if q be the maximum number of times an output pattern is repeated then minimum number of garbage bits required to ensure reversibility is $\log_2(q)$.

D. Quantum Cost

The quantum cost of a reversible gate is the number of elementary quantum gates needed to implement the gate. Elementary quantum gates are the elementary building block, like Not gate, Cnot gate, Controlled-V, Controlled-V + Rotation gates etc. Actually all (1 x 1) and (2 x 2) gates are considered as elementary quantum gates and the cost of all elementary quantum gates are considered as one.

E. Transistor Cost

In CMOS technology the reversible gates can be realized by transistors. The transistor cost (*TrC*) of a *TOFn* is given by $8.n$ where n is the number and that of Cnot gate is 8. TrC for generalized Fredkin gate is $8 * (n + 1)$ where n is number of control lines. Thus the *TrC* of usual Fredkin gate is 16.

F. Total cost

A circuit is considered better than another circuit (designed for the same computational task) if it has lesser number of garbage bits, circuit cost and quantum cost. But it is often observed that reduction of circuit cost leads to increase in garbage bits and reduction of quantum cost leads to increase in circuit cost. Keeping these in mind

we have introduced a new parameter called Total cost (TC) which is the sum of gate count of an optimized circuit, number of garbage bits and quantum cost.

G. Delay

Delay is considered as an important measure to evaluate a logic design. Kaye has defined that a reversible circuit design can be visualized as a sequence of discrete time slices and depth is summation of total time slices. Mohammadi and Eshghi have reported that delay is directly proportional to depth. Interestingly, Maslov et al. has prescribed a level compaction algorithm to optimize the depth of a circuit (level compaction). The protocol provides minimal delay.

III. PREVIOUS WORK

A. Majumder, P. L. Singh, N. Mishra, A. J. Mondal and B. Chowdhury,[1] As the conventional irreversible logic dissipates power for losing bits of information, computing engines has to be designed that do not require energy dissipation but only if computation is done logically reversible. Hence, research on reversible logic has been extensively increased now-a-days for its application in Quantum Computing, nanotechnology; QCA and Low power VLSI etc. In this research work, we have realized a Quantum Cost efficient Reversible RAM (RRAM) with a new 3×3 Reversible Gate named Modified Fredkin (MF). While approaching for RRAM we have also proposed a reversible D Flip-flop with minimum quantum cost (QC), a write enabled reversible master slave D Flip-flop & a $(i \times 2^i)$ reversible decoder which has outperformed the existing designs in terms of quantum cost, ancilla & garbage outputs. We also have analyzed the architectures in terms of logical depth (worst case delay), hardly addressed in available literature.

S. Nowrin, L. Jamal and H. Tasnim,[2] Power saving circuits are the need of the modern technology which can be achieved by using reversible logic. In this research work, we propose an efficient design of a reversible $n \times n$ signed multiplier circuit, where n is the number of bits of each operand of the multiplier. We propose a novel architecture of a generalized reversible compressor to reduce the number of partial products. Two algorithms have been presented to construct the Partial Product Generation (PPG) circuit and the Multi Operand Addition (MOA) circuit of the proposed multiplier. Our proposed design of MOA circuit needs only two steps to get the final output which is much optimized than existing Wallace Tree multiplier. During the realization process of the multiplier, two new gates have been proposed named as LS gate and LN gate to speed up the generation of partial products. In addition, several theorems on the numbers of gates, garbage outputs, and quantum cost of the reversible signed multiplier have been presented to show its efficiency. The comparative study shows that our proposed design is much better than the existing approaches in terms of numbers of gates, garbage outputs, quantum cost and delay. The simulation of the proposed circuit verifies the correctness of the design.

L. Gopal, N. S. Mohd Mahayadin, A. K. Chowdhury, A. A. Gopalai and A. K. Singh,[3] In low power circuit design, reversible computing has become one of the most efficient and prominent techniques in recent years. In this research work, reversible Arithmetic and Logic Unit (ALU) is designed to show its major implications on the Central Processing Unit (CPU). In this research work, two types of reversible ALU designs are proposed and verified using Altera Quartus II software. In the proposed designs, eight arithmetic and four logical operations are performed. In the proposed design 1, Peres Full Adder Gate (PFAG) is used in reversible ALU design and

HNG gate is used as an adder logic circuit in the proposed ALU design 2. Both proposed designs are analysed and compared in terms of number of gates count, garbage output, quantum cost and propagation delay.

H. Thapliyal and A. P. Vinod,[4] This paper presents the novel designs of reversible sequential circuits (latches and flip flops). The proposed reversible latches and flip flops are designed from reversible Fredkin, Feynman and Toffoli gates. Two new reversible gates called modified Fredkin gate (MFG) and modified Toffoli gate (MTG) are also proposed to design the optimized implementations. The proposed designs are better than the recently proposed ones in terms of number of reversible gates and garbage outputs. In order to reach towards the goal of transistor implementations of proposed reversible sequential circuits, transistor implementation of the existing Feynman gate, Fredkin gate, Toffoli gates as well as the proposed MTG and MFG are also proposed. The proposed transistor implementations are completely reversible in nature, i.e., suitable for both the forward and backward computation.

P. S. Phaneendra, C. Vudadha, V. Sreehari and M. B. Srinivas[5] Reversible computing has emerged as promising technology having its applications in emerging technologies like quantum computing, optical computing etc. This research work presents a reversible comparator based on prefix tree grouping methodology. The proposed design is realized by cascading three stages. The first stage is a 1-bit reversible comparator which generates 'greater' and 'equal' signals of that operand bit. These signals are combined using prefix tree grouping logic to generate final 'greater' and 'equal' signals. Using these final 'greater' and 'equal' signals, 'lesser' signal is generated in the third stage. The design is optimized in quantum level for efficient performance in all the cost metrics. The proposed 64-bit comparator design results in 14.3% reduced quantum delay, 7.8% reduced quantum cost and 25% reduced garbage outputs when compared with the best existing design of prefix based comparator.

H. M. H. Babu, L. Jamal and N. Saleheen [6] Reversible logic has captured significant attention in recent time as reducing power consumption is the main concern of digital logic design. It consumes less power by recovering bit loss from its unique input-output mapping. This research work presents the design of an optimal reversible fault tolerant carry look-ahead adder. The comparative study shows that the proposed design is much better than the existing approach considering all the efficiency parameters of reversible circuit design which includes numbers of gates, quantum cost, delay, quantum gate complexity and garbage outputs. The proposed 8-bit reversible fault tolerant carry look-ahead adder improves 94.9% on the number of gates, 92.4% on the quantum cost, 93.2% on the garbage outputs and 14.5% on the delay than the existing design.

IV. CONCLUSION

Throughout the brief study and The basic principle of reversible computing is that a objective device with an identical number of input and output lines will produce a computing environment where the electrodynamics of the system allow for prediction of all future states based on known past states, and the system reaches every possible state, resulting in no heat dissipation. The novel reversible realization and optimization of RRAM will play a big role to reversible logic community to work further for the design of a synchronous N-bit dual-port SRAM array and DRAM array for their application in FPGA or Network-on-chip.in the proposed work using the same reversible logic we are implementing a 3:8 decoder RRAM.

REFERENCES

- [1] Majumder, P. L. Singh, N. Mishra, A. J. Mondal and B. Chowdhury, "A novel delay & Quantum Cost efficient reversible realization of $2^i \times j$ Random Access Memory," 2015 International Conference on VLSI Systems, Architecture, Technology and Applications (VLSI-SATA), Bangalore, 2015, pp. 1-6.
- [2] S. Nowrin, L. Jamal and H. Tasnim, "An efficient approach to design a reversible signed multiplier," TENCON 2014 - 2014 IEEE Region 10 Conference, Bangkok, 2014, pp. 1-6.
- [3] L. Gopal, N. S. Mohd Mahayadin, A. K. Chowdhury, A. A. Gopalai and A. K. Singh, "Design and synthesis of reversible arithmetic and Logic Unit (ALU)," 2014 International Conference on Computer, Communications, and Control Technology (I4CT), Langkawi, 2014, pp. 289-293.
- [4] P. S. Phaneendra, C. Vudadha, V. Sreehari and M. B. Srinivas, "An Optimized Design of Reversible Quantum Comparator," 2014 27th International Conference on VLSI Design and 2014 13th International Conference on Embedded Systems, Mumbai, 2014, pp. 557-562.
- [5] H. M. H. Babu, L. Jamal and N. Saleheen, "An efficient approach for designing a reversible fault tolerant n-bit carry look-ahead adder," 2013 IEEE International SOC Conference, Erlangen, 2013, pp. 98-103.
- [6] M. Morrison, M. Lewandowski, R. Meana and N. Ranganathan, "Design of static and dynamic RAM arrays using a novel reversible logic gate and decoder," 2011 11th IEEE International Conference on Nanotechnology, Portland, OR, 2011, pp. 417-420.
- [7] Sk. Noor Mahammad and Kamakoti Veezhinathan, "Constructing Online Testable Circuits Using Reversible Logic", IEEE transactions on instrumentation and measurement, vol. 59, no. 1, January 2010.
- [8] H. Thapliyal, A. P. Vinod, "Design of reversible sequential elements with feasibility of transistor implementation" ' In Proceedings of the IEEE international Symposium on Circuits and System, 625-628,2007.
- [9] R. Landauer, "Irreversibility and heat generation in the computational process", IBM Journal of Research. Dev. 5, 183-191, 1961.
- [10] C. H. Bennett, R. Landauer, "The fundamentals physical limits of computation".
- [11] C. H. Bennett, "Logical reversibility of computation", IBM Journal of Research. Devel. 17, 525-532, 1973.
- [12] Tommaso Toffoli, "Reversible Computing,' Automata, Languages and Programming, 7th Colloquium of Lecture Notes in Computer Science, vol. 85, pp. 632-644, 1980.